The Beatles use the major mediant (III) 62 times in 18 tracks:

III: 3  
  approach: I x3  
  progress: vi x3

[5] 'There's A Place'
III: 2  
  approach: I x2  
  progress: vi x2

[21] 'I Want to Hold Your Hand'
III: 9  
  approach: V x1, vi x8  
  progress: I x4, IV x5

[22] 'This Boy'
III: 1  
  approach: IV x1  
  progress: vi x1

[24] 'You Can't Do That'
III: 4  
  approach: I x4  
  progress: vi x4

[26] 'I Should Have Known Better'
III: 4  
  approach: I x2, IV x2  
  progress: vi x4

[29] 'I'm Happy Just To Dance With You'
III: 5  
  approach: Ø x5  
  progress: IV x5

[40] 'I Don't Want to Spoil the Party'
III: 5  
  approach: vi x5  
  progress: ii x5

[42] 'No Reply'
III: 2  
  approach: I x2  
  progress: VI x2

[50] 'Yes It Is'
III: 1  
  approach: I x1  
  progress: IV x1

[59] 'Yesterday'
III: 8  
  approach: I x4, vii x4  
  progress: vi x8

[114] 'All You Need Is Love'
Their approach and progress break down as follows:

APPROACH:

Ø: 6 instances (9.7%) in 2 songs
- x5 [29] 'I'm Happy Just To Dance With You'
- x1 [146] 'Birthday'

I: 31 instances (50.0%) in 12 songs
- x3 [4] 'Ask Me Why'
- x2 [5] 'There's A Place'
- x4 [24] 'You Can't Do That'
- x2 [26] 'I Should Have Known Better'
- x2 [42] 'No Reply'
- x1 [50] 'Yes It Is'
- x4 [59] 'Yesterday'
- x4 [114] 'All You Need Is Love'
- x1 [147] 'Piggies'
• x2  [173] 'You Never Give Me Your Money'
• x3  [175] 'Golden Slumbers'
• x3  [178] 'Maxwell's Silver Hammer'

ii: 2 instances (3.2%) in 1 song
• x2  [147] 'Piggies'

IV: 3 instances (4.8%) in 2 songs
• x1  [22] 'This Boy'
• x2  [26] 'I Should Have Known Better'

V: 3 instances (4.8%) in 2 songs
• x1  [21] 'I Want to Hold Your Hand'
• x2  [151] 'Martha My Dear'

vi: 13 instances (21.0%) in 2 songs
• x8  [21] 'I Want to Hold Your Hand'
• x5  [40] 'I Don't Want to Spoil the Party'

vii: 4 instances (6.5%) in 1 song
• vii x4  [59] 'Yesterday'

PROGRESS:

I: 5 instances (8.1%) in 2 songs
• x4  [21] 'I Want to Hold Your Hand'
• x1  [146] 'Birthday'

ii: 6 instances (9.7%) in 2 songs
• x5  [40] 'I Don't Want to Spoil the Party'
• x1  [147] 'Piggies'

IV: 13 instances (21.0%) in 5 songs
• x5  [21] 'I Want to Hold Your Hand'
• x5  [29] 'I'm Happy Just To Dance With You'
• x1  [50] 'Yes It Is'
• x2  [147] 'Piggies'

VI: 2 instances (3.2%) in 1 song
• x2  [42] 'No Reply'

vi: 36 instances (58.1%) in 11 songs
• x3  [4] 'Ask Me Why'
• x2  [5] 'There's A Place'
• x1  [22] 'This Boy'
• x4  [24] 'You Can't Do That'
• x4  [26] 'I Should Have Known Better'
• x8  [59] 'Yesterday'
• x4  [114] 'All You Need Is Love'
• x2  [151] 'Martha My Dear'
• x2  [173] 'You Never Give Me Your Money'
• x3  [175] 'Golden Slumbers'
• x3  [178] 'Maxwell's Silver Hammer'